# EXERCISE 4: Utility Maximization and Expenditure Minimization 

Part 1. Exercises 2.D.3, 3.D.4, 3.D.5 (a - c), 3.D.6, 3.E.4, 3.E.6, 3.E.7, 3.E.8 (plot indirect utility as a function of $w$ and expenditure as a function of $u$ ).

Part 2.

Let $X=\mathbb{R}_{+}^{2}$ and let preferences be represented by the following utility functions:

$$
\begin{gathered}
u\left(x_{1}, x_{2}\right)=\min \left\{3 x_{1}+x_{2}, 2 x_{2}\right\} \\
u\left(x_{1}, x_{2}\right)=\max \left\{\alpha x_{1}, \beta x_{2}\right\} \quad, \quad \alpha>0, \beta>0 \\
u\left(x_{1}, x_{2}\right)=\max \left\{\alpha x_{1}, \alpha x_{2}\right\}+\min \left\{x_{1}, x_{2}\right\} \quad, \quad \alpha>0
\end{gathered}
$$

Derive the Walrasian and Hicksian demand, indirect utility and expenditure functions.

